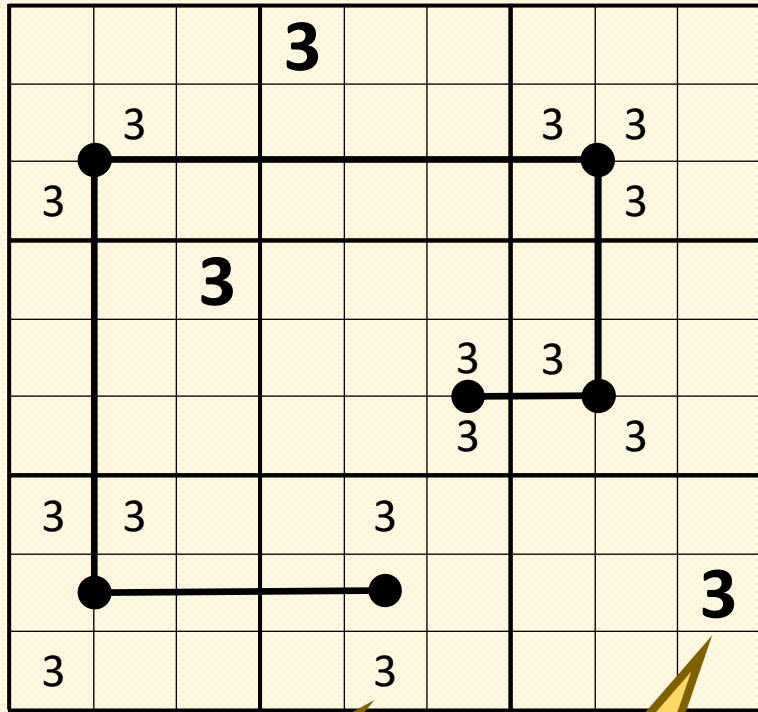


# Serpentine Technique

---

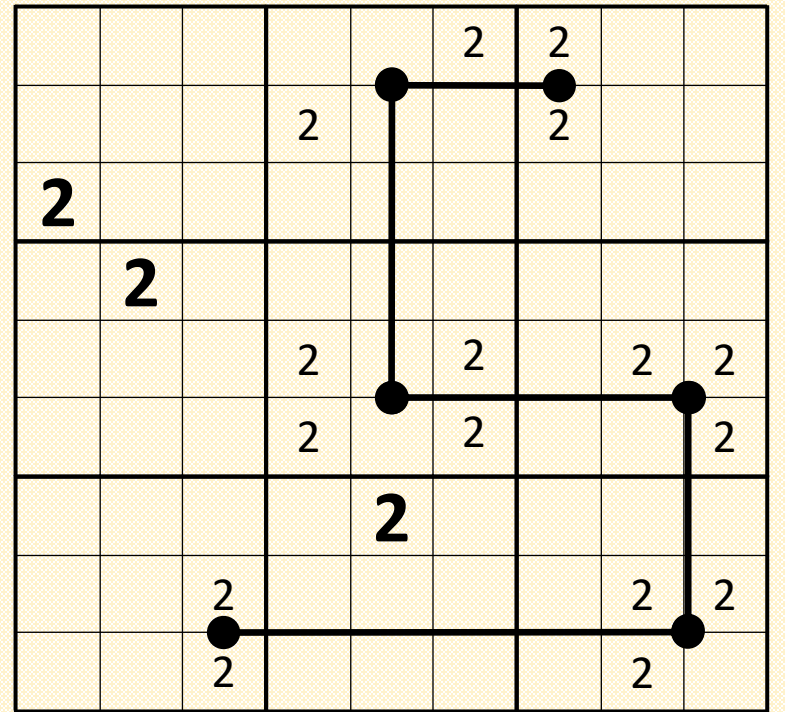
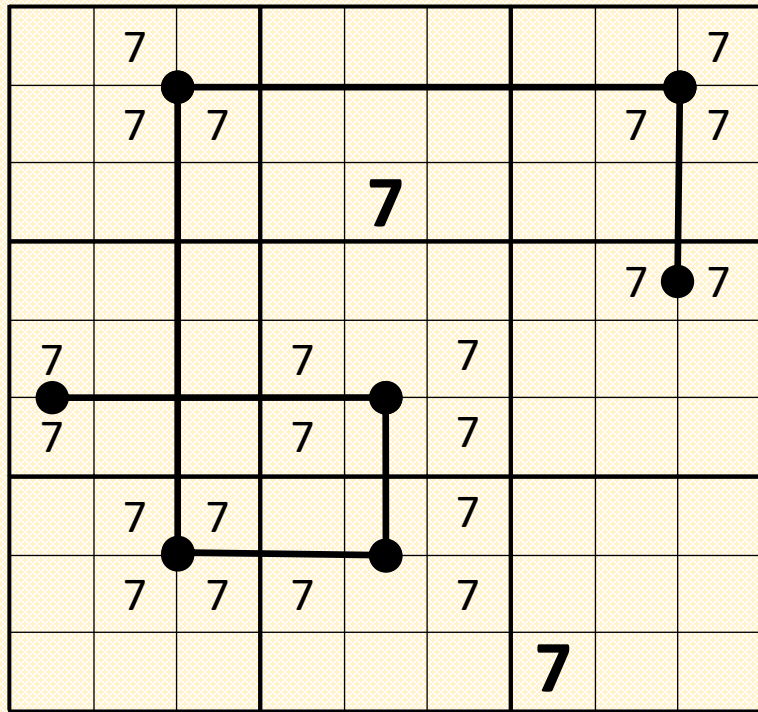
For the solution of Sudoku Puzzles

Vers. 3

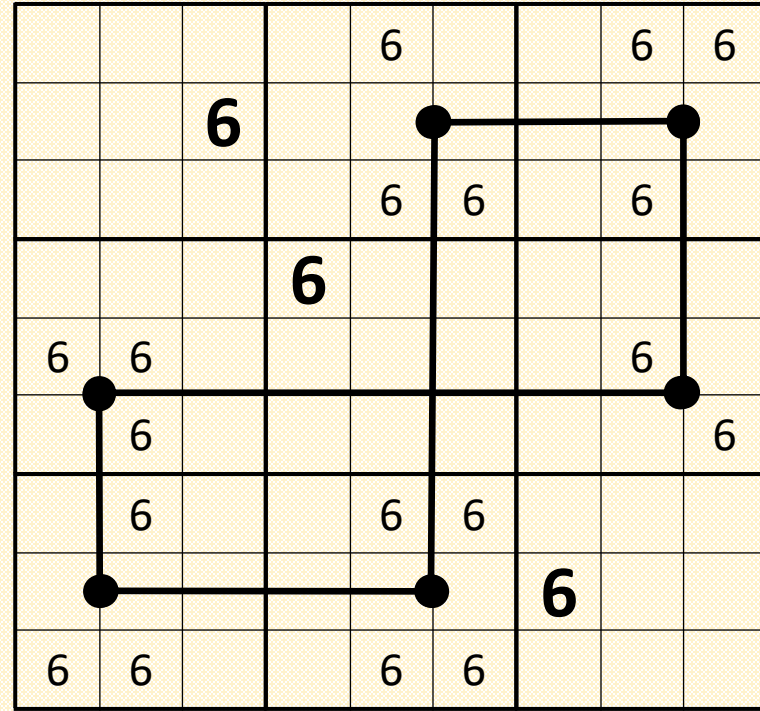
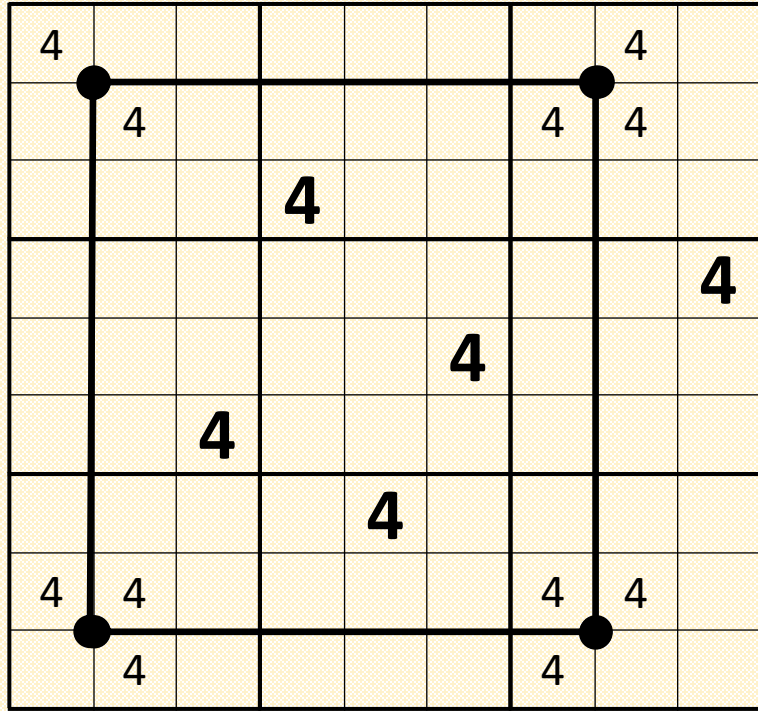
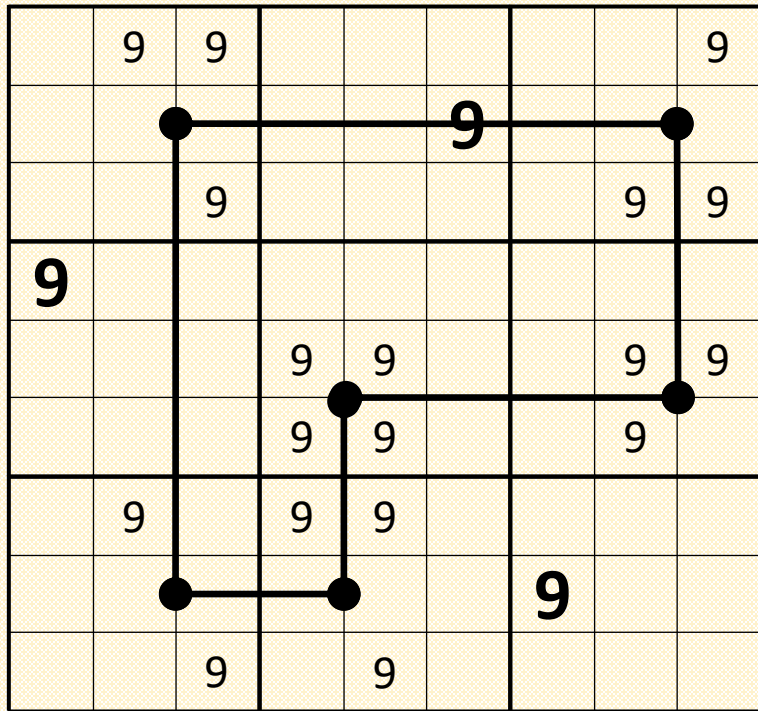


Possible Candidate

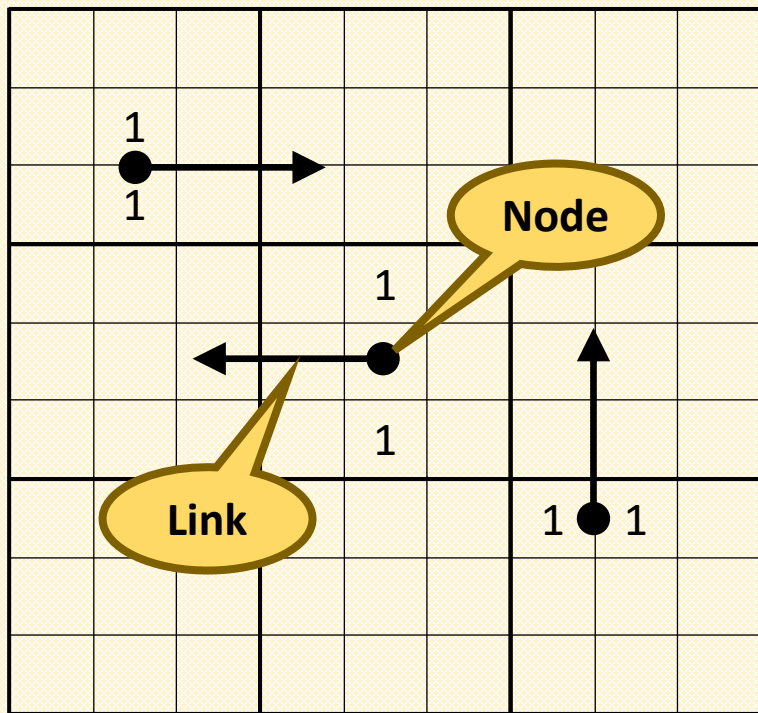
Already Completed



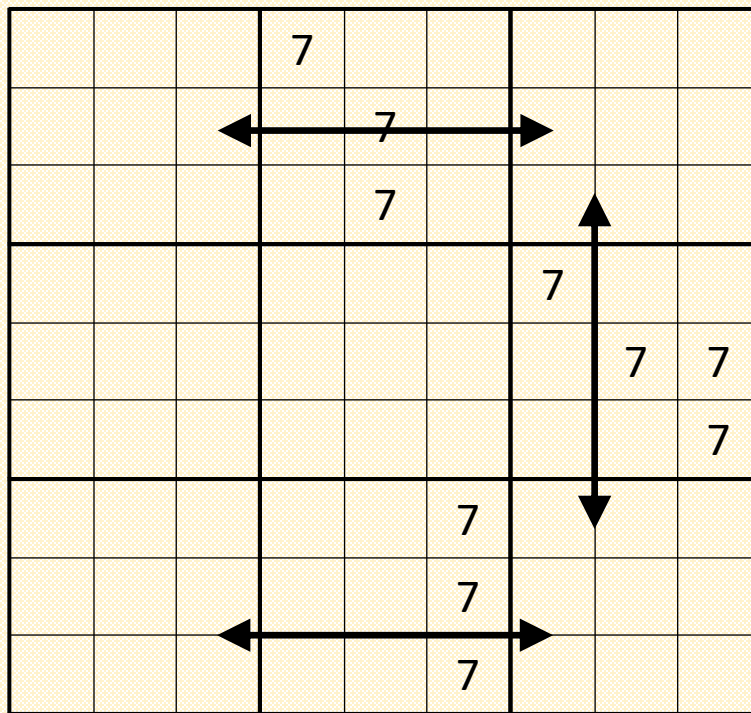
# TYPICAL SERPENTS



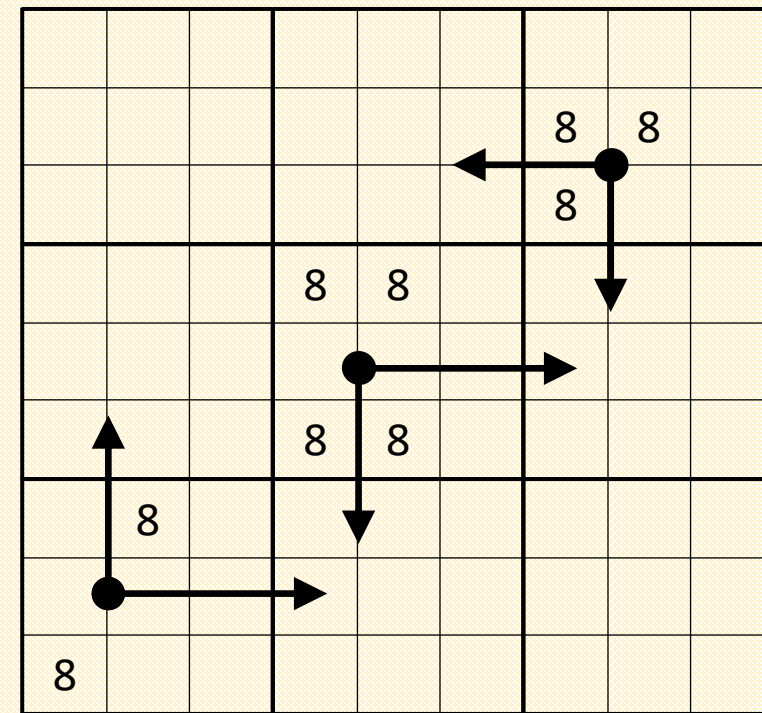
**TYPICAL TAIL-BITING SERPENTS**



**Heads or tails**



**Passthroughs**



**Turners**

N.B. those formed of 3 or 4 cells can become heads or tails.

**PARTS OF A SERPENT**

3	•			4	4		5	5
	3				4			•
								5
6			9	9		7		7
	•		9	•			•	7
		6	9					
	8		1	1			2	
8	•	•	1	•	1		•	•
						2		2

Possible Turning Nodes

5		5	6	6		7	7	
	•		6	•	6		7	•
			6	•	6		7	•
5		5	6	6		7		
8	8	8		9	9			1
	•	•	•		•		•	•
	•	•	8				•	•
8	8	8		9	9	1	1	1

Possible Turning Nodes

2	•	2						
				3	•	3		
							4	•
							•	•
5				6				7
•								•
5				•				•
				6				•
								7

Possible Head and Tail Nodes

Possible nodes are an aid to identifying serpents.

**POSSIBLE NODES**

# TECHNIQUE

## **BEGIN BY USING THESE SIMPLE TECHNIQUES**

1. Candidates are numbers that a cell might contain. Firstly, look for and complete cells with obvious single candidates.
2. Note the possible candidates for every cell that remains empty.
3. If for any major square a candidate only appears in a single row or column, then this candidate can be deleted from the same row or column where it passes through the other two major squares.
4. If a candidate appears in only two rows or columns in a major square and only the same two rows or columns as the pass through a second major square, then it can be deleted from the same two rows or columns as they pass through the third major square.
5. Look for two cells in a row, column or major square that have the same two candidates. Delete those candidates from the other cells in that row, column or major square.
6. Repeat step 3 for three cells with the same three candidates.
7. If no further progress can be made using the above techniques, then move on to the serpentine approach.

## **MOVE ON TO THE SERPENTINE APPROACH IF NECESSARY.**

1. For each number mark the cells for which it is a candidate in a separate grid.
2. Check for any X-Wings or Clashes as described in the examples.
3. Find the longest serpent, i.e., one that covers as many major squares in the grid as possible. Serpents that are biting their tails (i.e., that form loops) are preferable. Identifying possible turner nodes in each major square helps to identify serpents.
4. Delete the candidate from cells that are not a part of the serpent, as described in the examples.
5. Further simplify the remaining candidates, as described in the examples.
6. In some cases, this will enable you to complete a cell. In other cases, it will remove one of two candidates from a cell leaving just one candidate. In yet other cases it will create simple pairs or triples.
7. Solution of the puzzle can then continue using the simple techniques described above.
8. If no further progress can be made try the serpentine technique again using another number.

<b>7</b>								
			7			7		<del>7</del>
					7			
	<b>7</b>							
			<del>7</del>	7	7			
							<b>7</b>	
			7			7		
		<b>7</b>						
			<del>7</del>		7			7

An X-Wing comprises four candidates that form a rectangle. Other candidates in the rows and columns occupied by an X-Wing can be deleted.

			4		4			
4							4	
4			4		4		4	

Arrangements of this type are ambiguous. Either one of the two sets of four candidates could be an X-Wing and they interfere with one another.

			4		4			
4							4	
4			<del>4</del>		<del>4</del>		4	
			4		4			

This arrangement is not ambiguous, however. The two sets of four candidates do not interfere with one another.

# X-WINGS 1

	8							8
					8			
		8				8		
							8	
8								
			8					
	<del>8</del>	8				8		
	8	<del>8</del>				<del>8</del>		8
				8				

M66

			4					
								4
	4							
					4	4		
				4	<del>4</del>	<del>4</del>	4	
4								
					4	4		
				4	<del>4</del>	<del>4</del>	4	
			4					

M66

		<del>4</del>			4	<del>4</del>		<del>4</del>
		4				<del>4</del>	<del>4</del>	
					<del>4</del>	<del>4</del>	4	4
				4		4	<del>4</del>	<del>4</del>
	4							
				4		4		
							4	4
4								
			4					

M71

Some apparent serpents can be combinations of X-Wings.  
So, this possibility must be checked first.

## X-WINGS 2



	<b>3</b>							
			3		3			
							<b>3</b>	
3						3		3
3		3				3		3
				<b>3</b>				
3		3	<del>3</del>					
		3	<del>3</del>			3		3
<del>3</del>			3		3	<del>3</del>		<del>3</del>

Step 1 – X-Wing

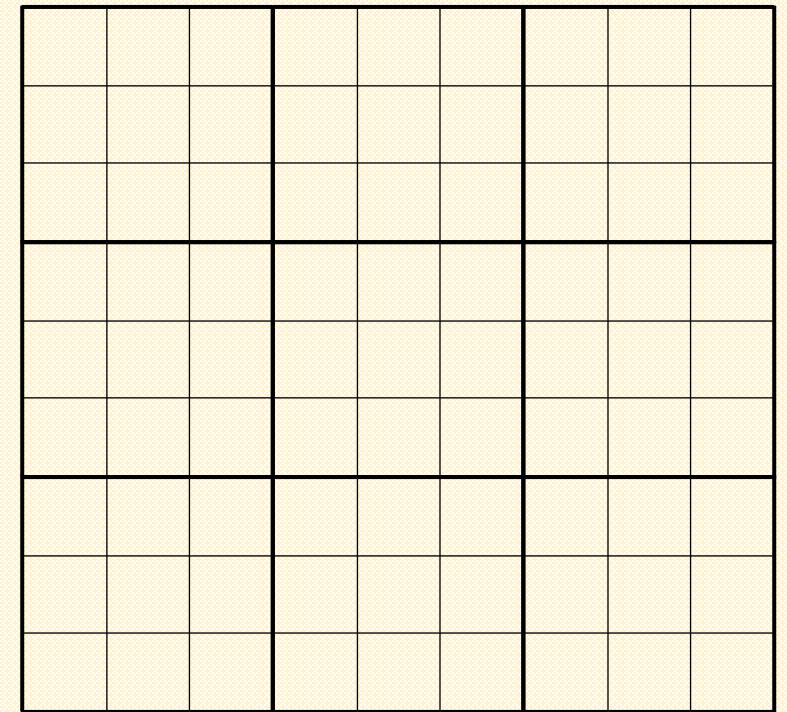
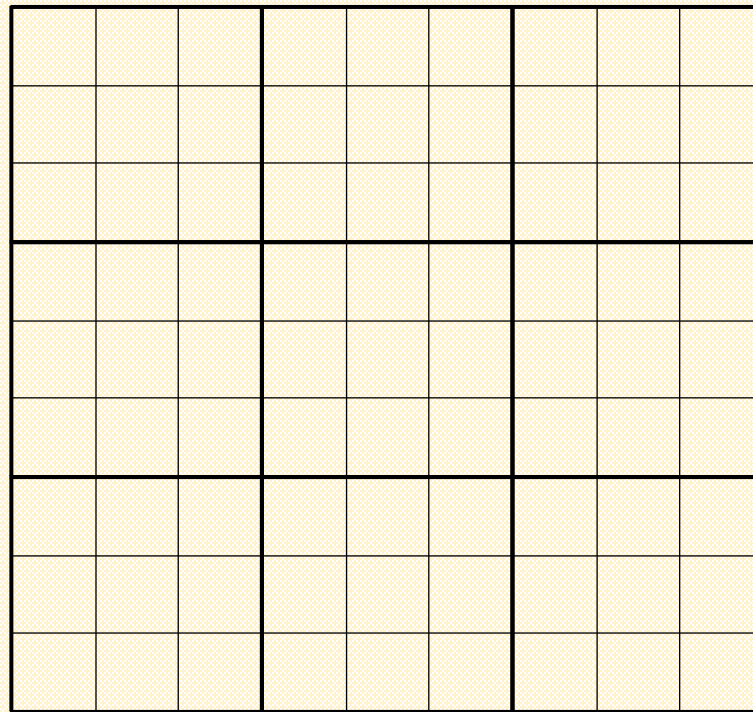
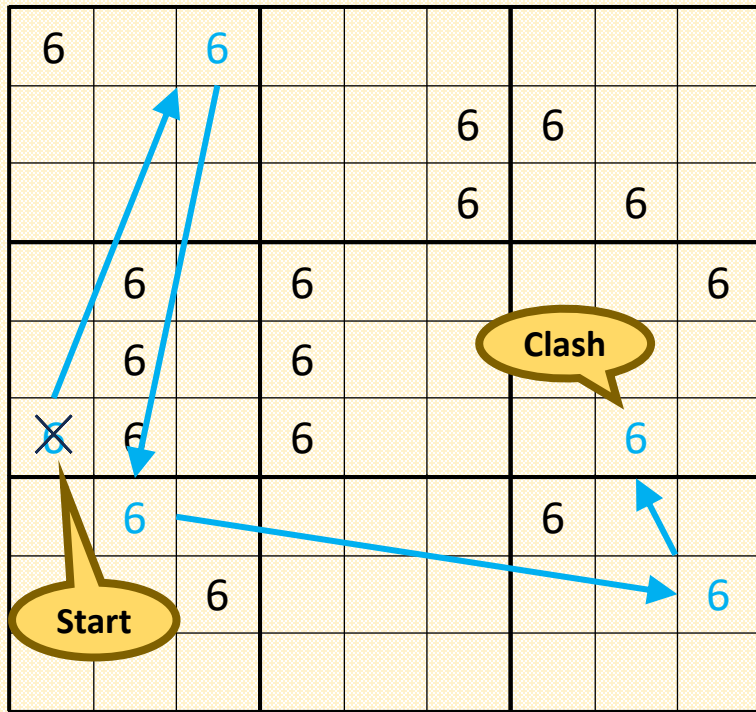
	<b>3</b>							
			3		3			
							<b>3</b>	
<del>3</del>						3		3
3		3				<del>3</del>		<del>3</del>
				<b>3</b>				
3		3						
		<del>3</del>				3		3
			3		3			

Step 2 – X-Wing

	<b>3</b>							
			3		3			
							<b>3</b>	
							3	3
3		3						
				<b>3</b>				
3		3						
							3	3
			3		3			

Final Result

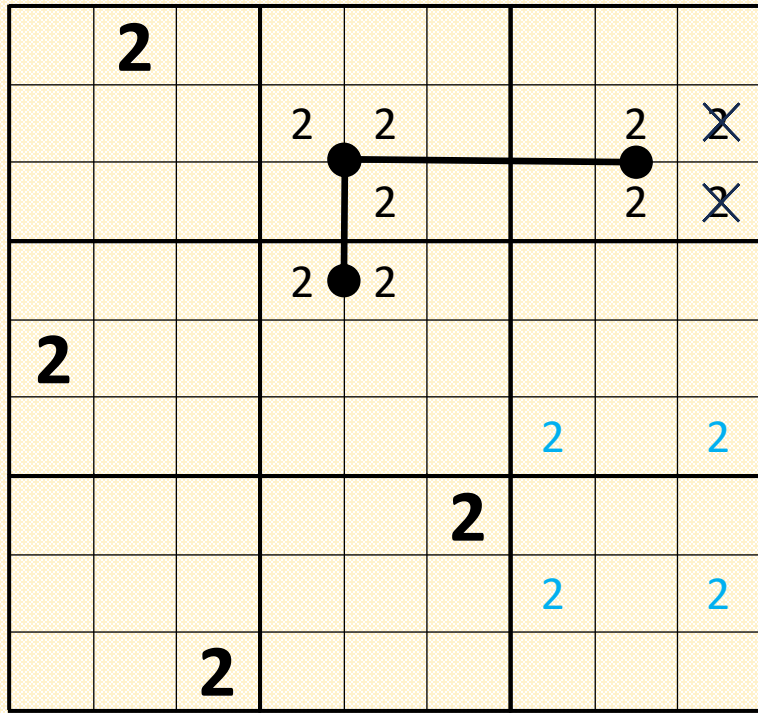
# X-WINGS 3



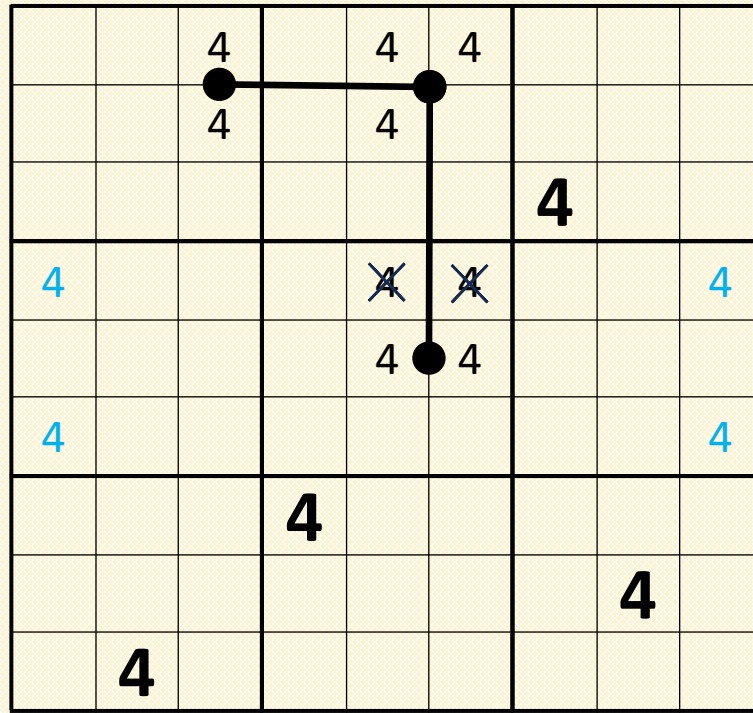
M72

6 can be deleted from the start  
Because tracing its effect through  
the grid results in a clash.

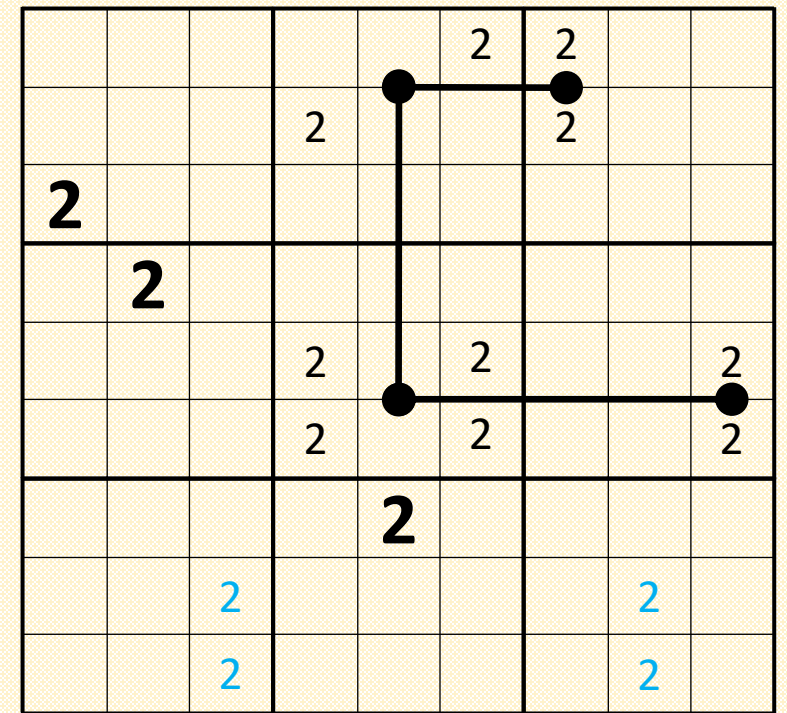
# CLASHES



M65

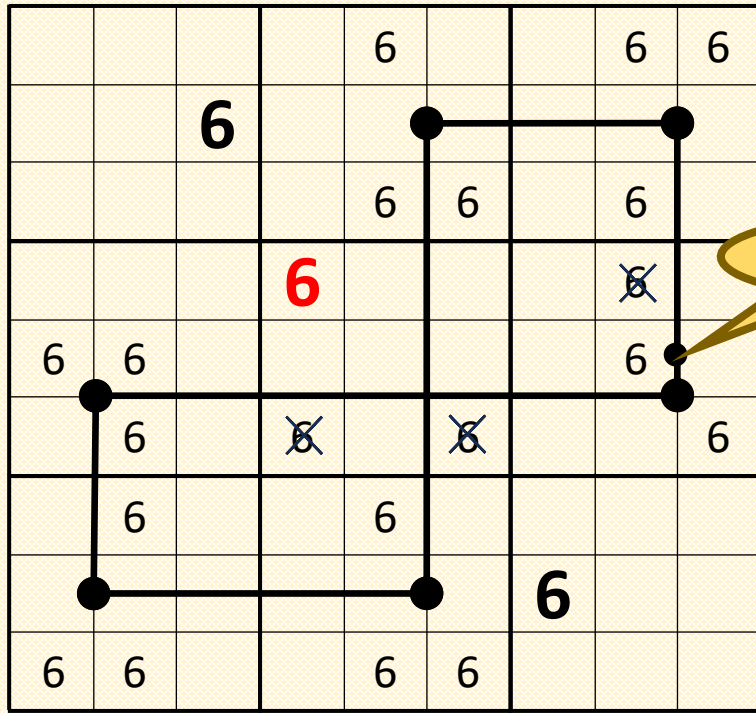


M63

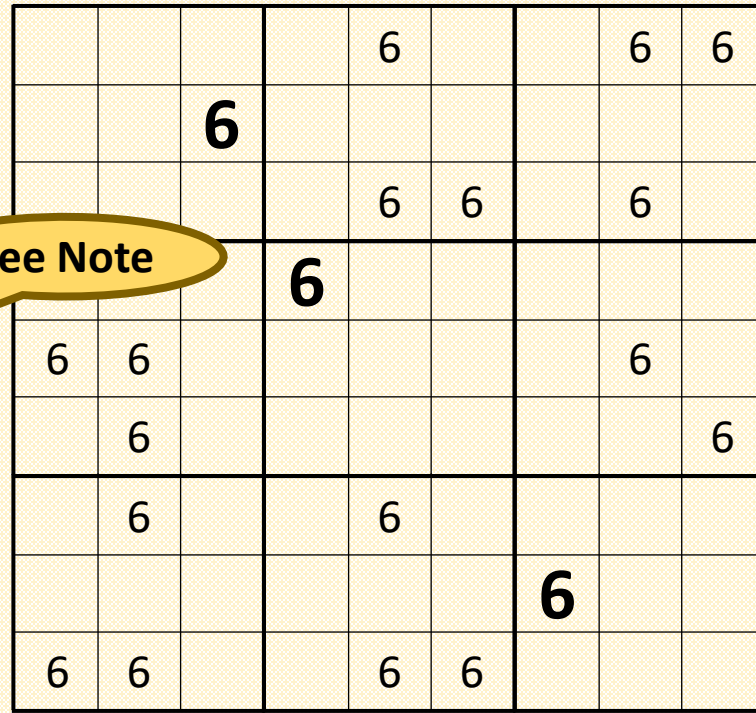


It is possible for a serpent and an X-wing to co-exist.  
But they must not interfere with one another.

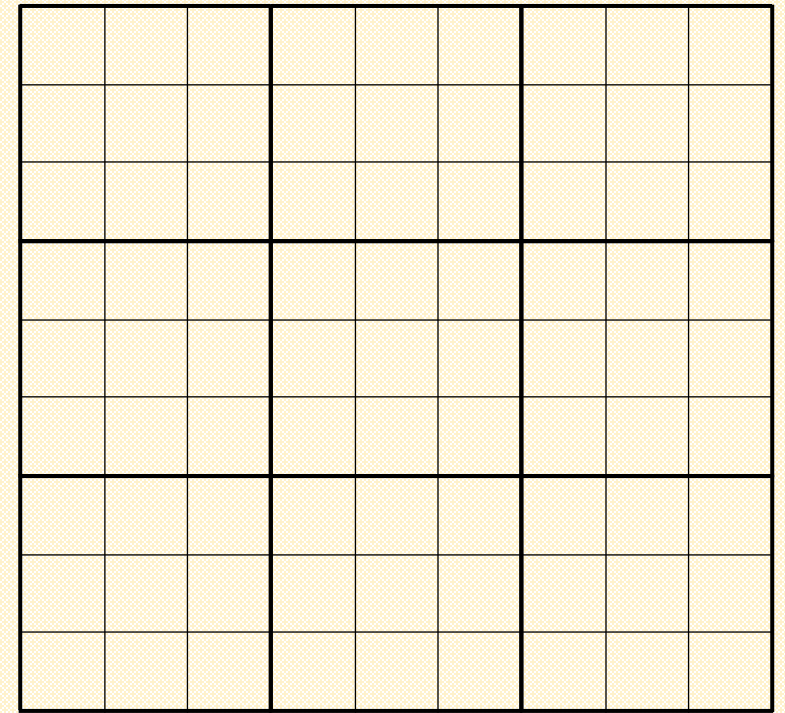
## X-WINGS & SERPENTS



See Note



Result



The red 6 is identified from the two passthroughs.  
 Note: The possible node ● is not used.

**SERPENT EXAMPLE 1**

			5	5			<del>5</del>	
5	5			•			5	
5	5		<del>5</del>					5
		<b>5</b>						
					<b>5</b>			
						<b>5</b>		
5							5	5
	•	5			<del>5</del>			5
		<del>5</del>		5	5			

Step 1 - Passthrough

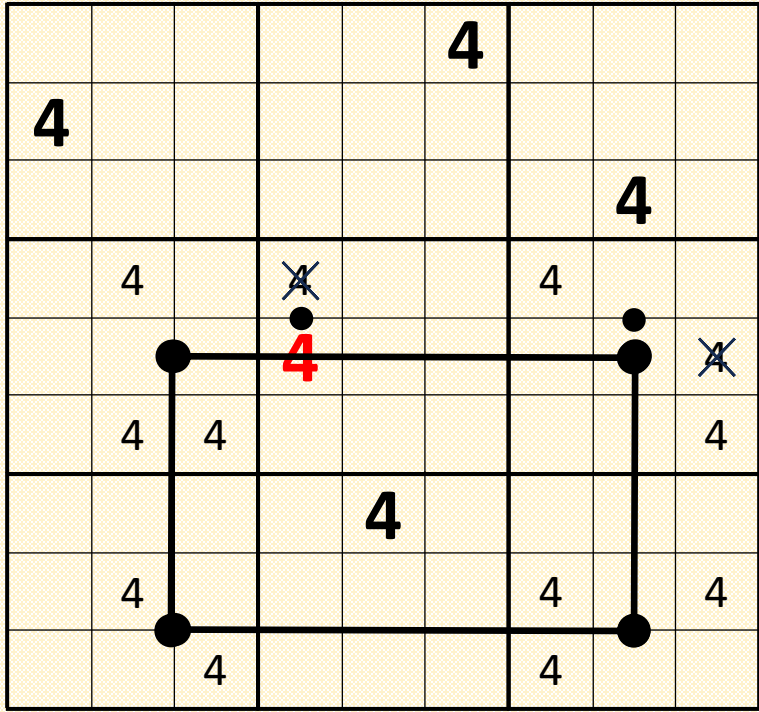
			5	5				
5	<del>5</del>						5	
<del>5</del>	5							5
		<b>5</b>						
					<b>5</b>			
						<b>5</b>		
5							5	<del>5</del>
	5							5
			5	5				

Step 2 - X-Wings

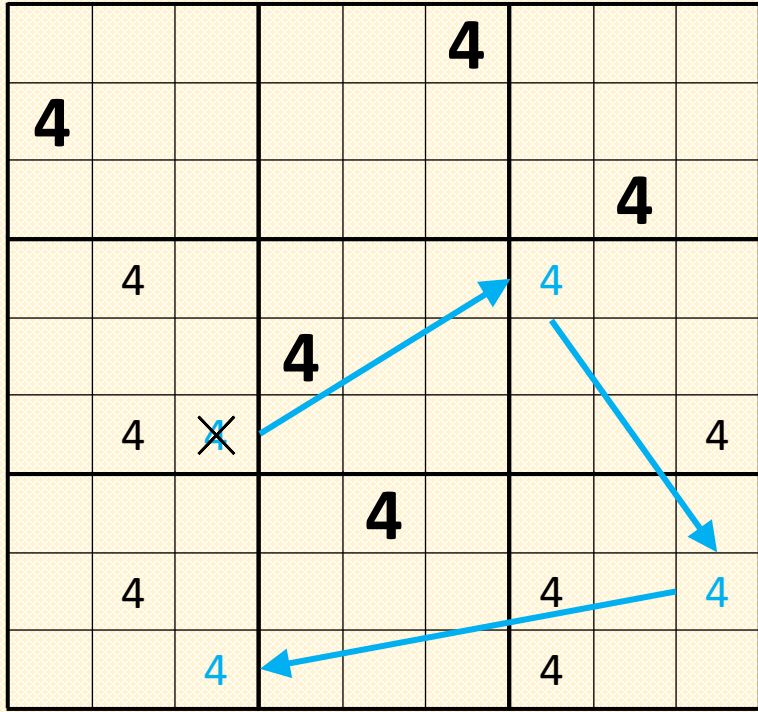
			5	5				
5								5
	5							5
		<b>5</b>						
					<b>5</b>			
						<b>5</b>		
5								5
	5							5
			5	5				

Result

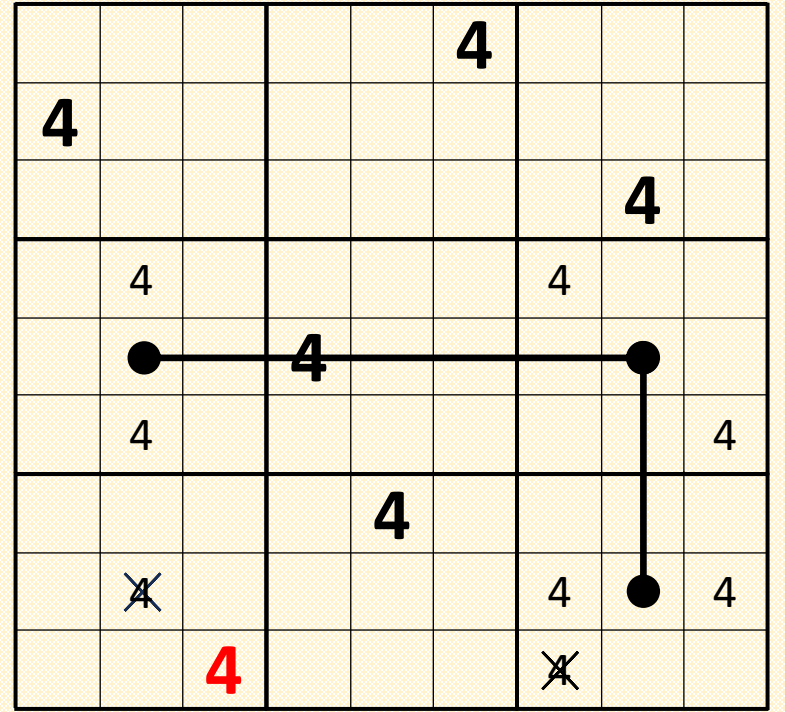
**SERPENT EXAMPLE 2**



Step 1 - Serpent

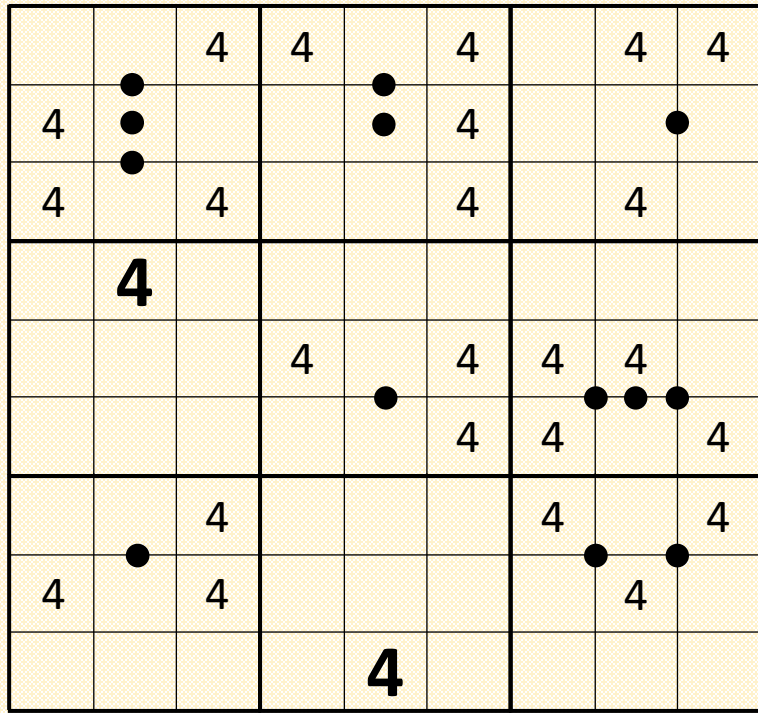


Step 2 - Eliminating Clashing Cells

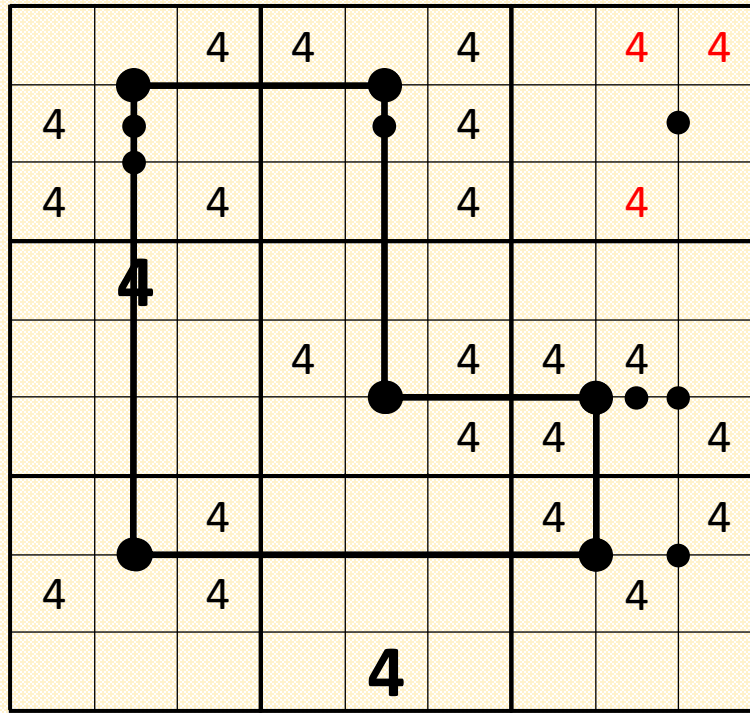


Step 3 - Complete Simplification

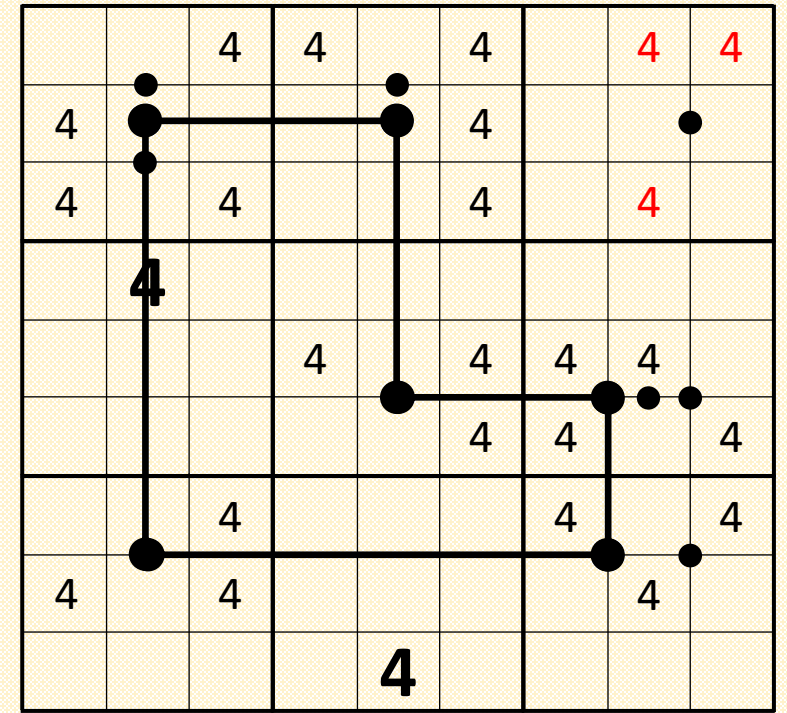
**SERPENT EXAMPLE 3**



Step 1 - Possible Nodes



N.B., this is not a possible serpent because all the red 4s would be deleted.



N.B., this is also not a possible serpent because all the red 4s would be deleted.

**SERPENT EXAMPLE 4**

		4	<del>X</del>		<del>X</del>		4	4
<del>X</del>	●	●	●	●	<b>4</b>	●	●	●
4	●	4			<del>X</del>	4		
	<b>4</b>							
			4	●	4	4	<del>X</del>	●
				4	4	●	●	<del>X</del>
	4				<del>X</del>	●	4	●
4	●	4				4	●	●
				<b>4</b>				

Step 2 - Only Possible Serpent

		4					4	4
					<b>4</b>			
4		4					4	
	<b>4</b>							
			<b>4</b>		<del>X</del>	<del>X</del>		
					<del>X</del>	<b>4</b>		
		4						4
4		4					4	
				<b>4</b>				

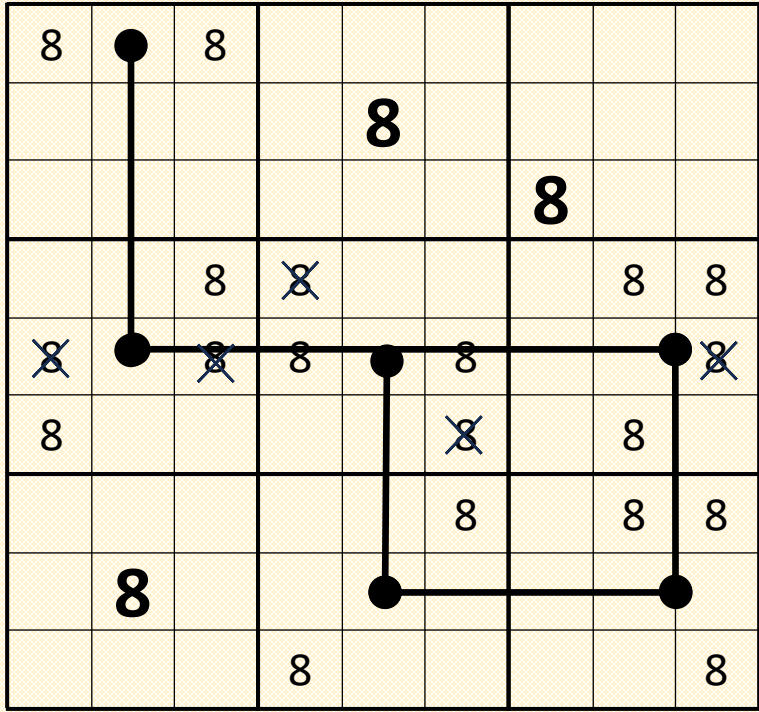
Step 3 - Continuation of solution

		4					<del>X</del>	4
					<b>4</b>			
4		<del>X</del>					4	
	<b>4</b>							
			<b>4</b>					
							<b>4</b>	
		4						4
4		<del>X</del>					4	
				<b>4</b>				

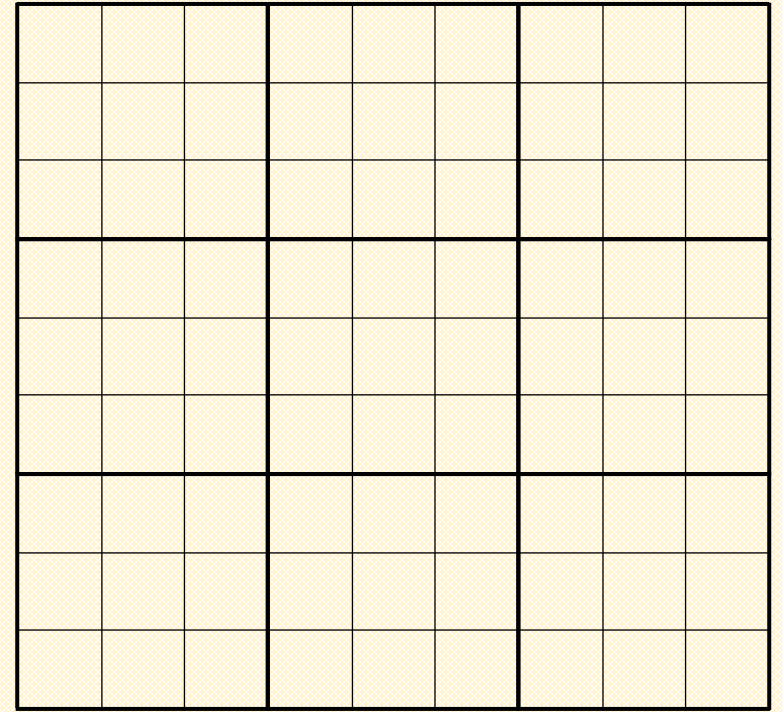
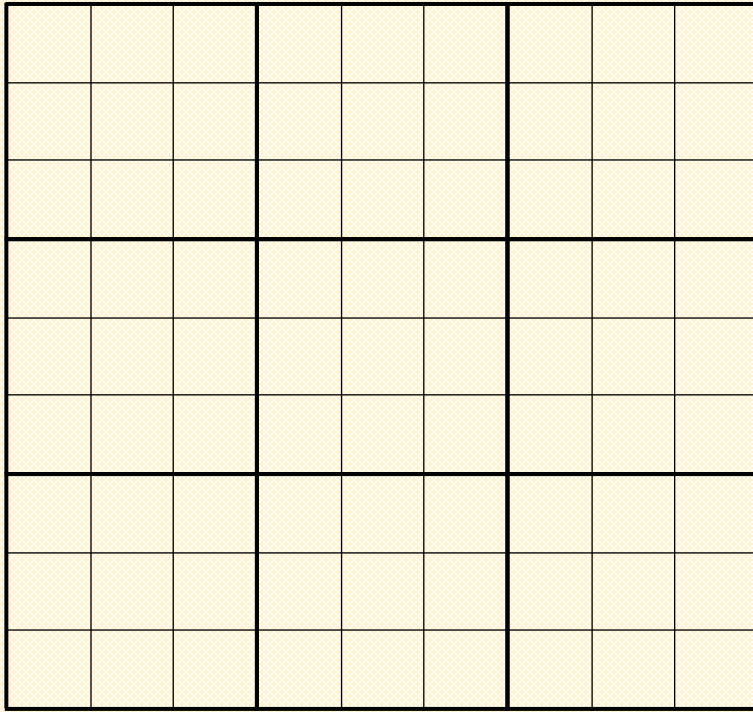
Step 4 - X-Wings

**SERPENT EXAMPLE 4 (Contd.)**

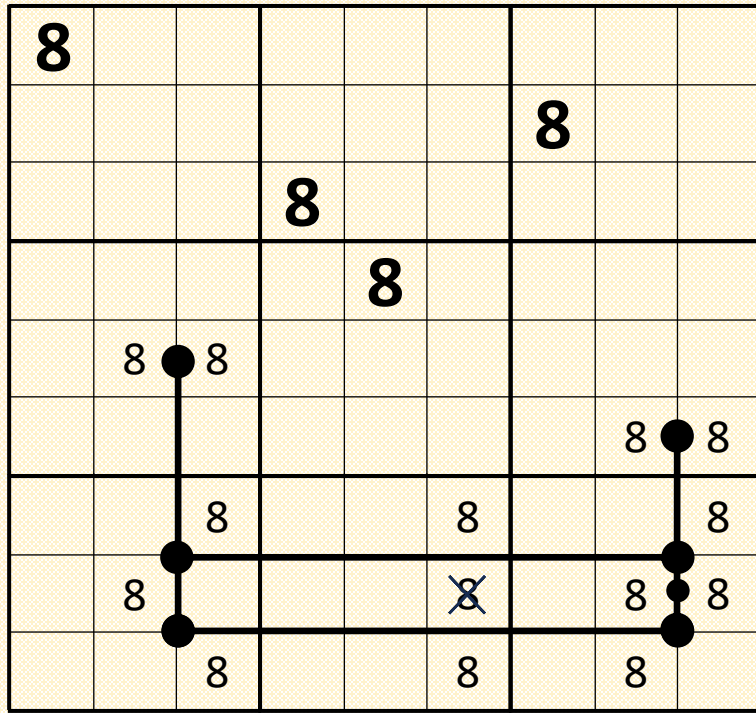




M63



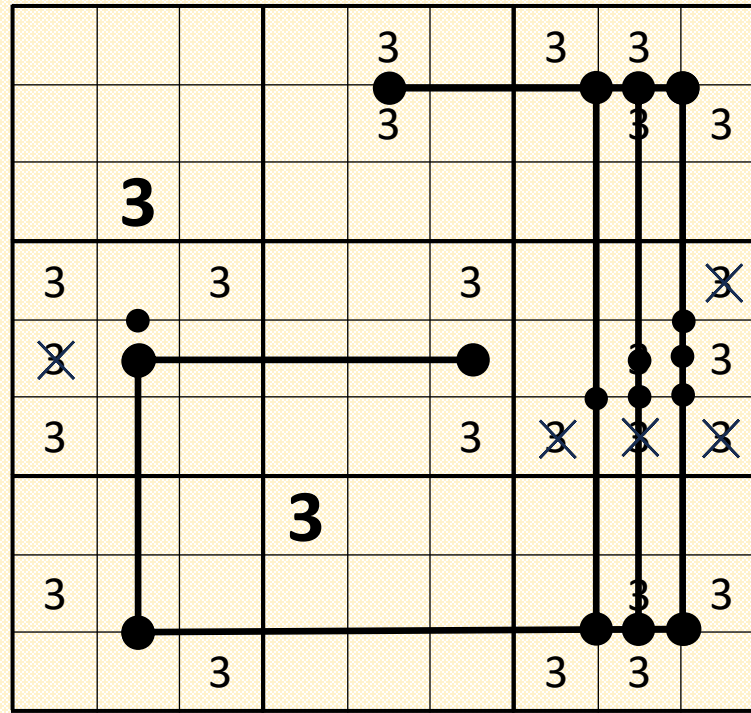
**SERPENT EXAMPLE 5**



**Double Passthroughs**

M43

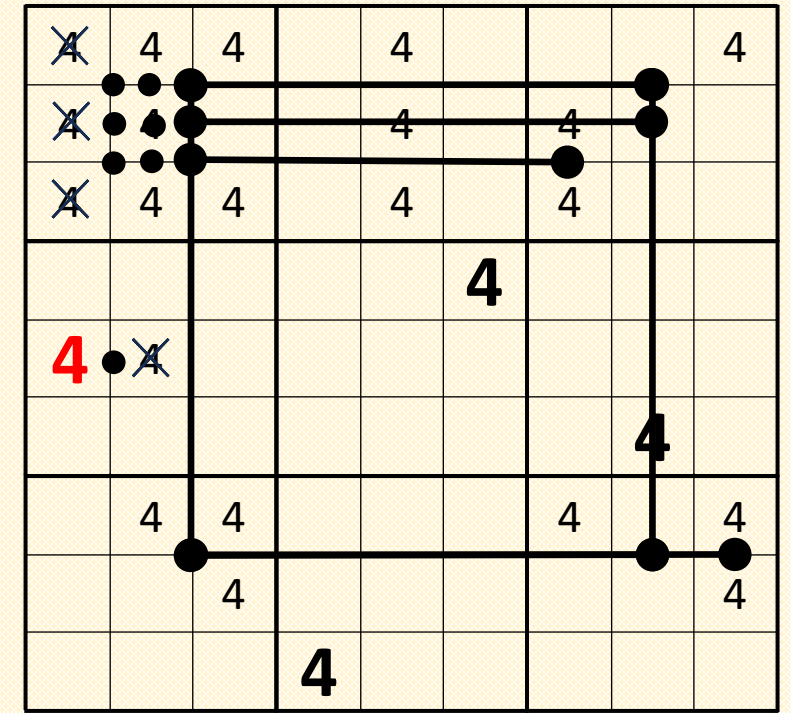
The top passthrough yields the bottom 8 and the bottom passthrough yields the top 8. So, the central 8 can be deleted.



**Passback**

M43

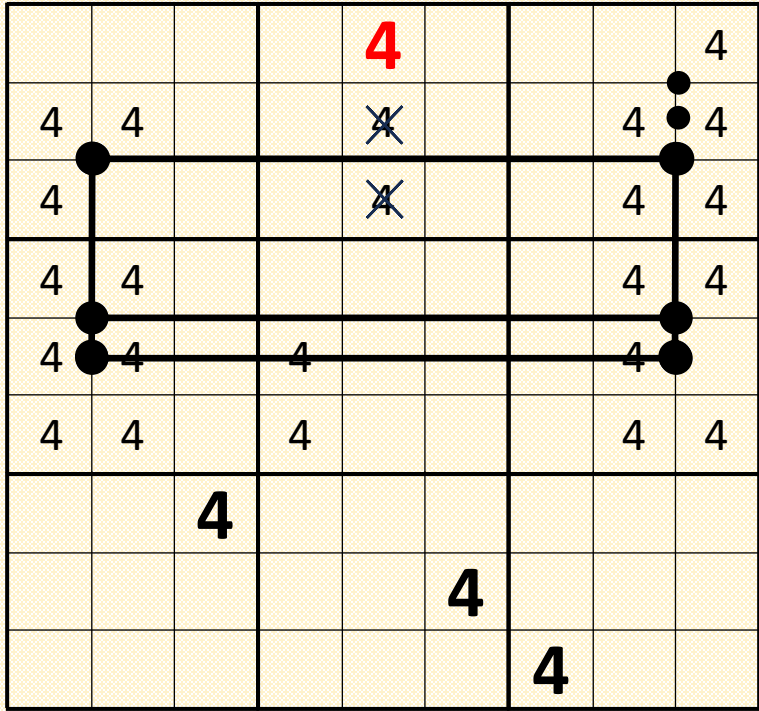
If all the possible serpents share common links, then these links can be used to delete candidates from cells.



**Passthrough**

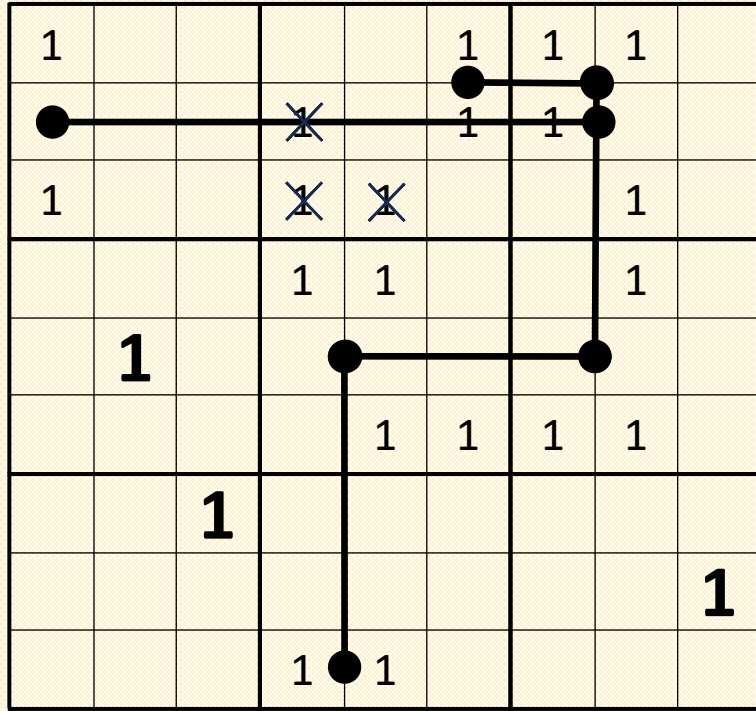
M53

**MULTIPLE SERPENTS 1**



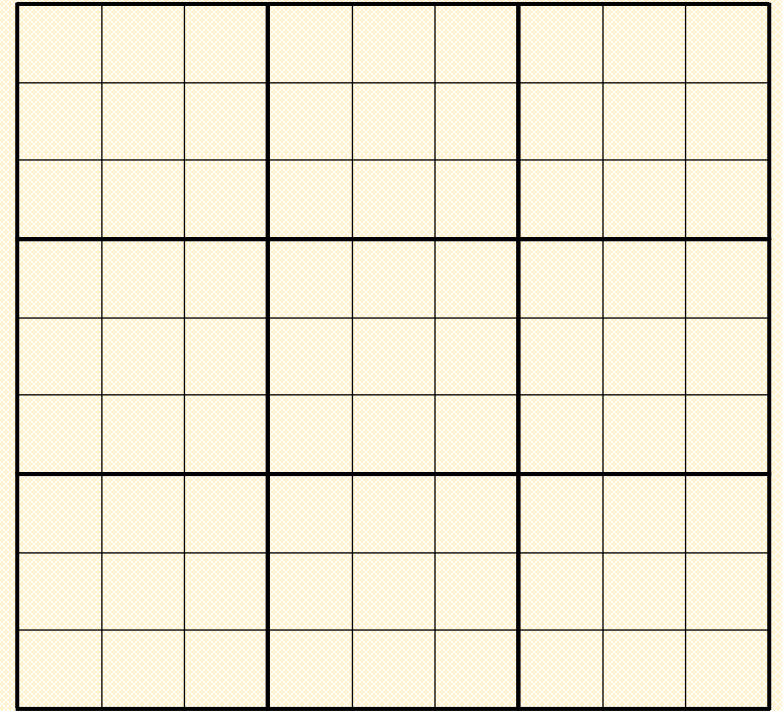
**Passthrough**

M64

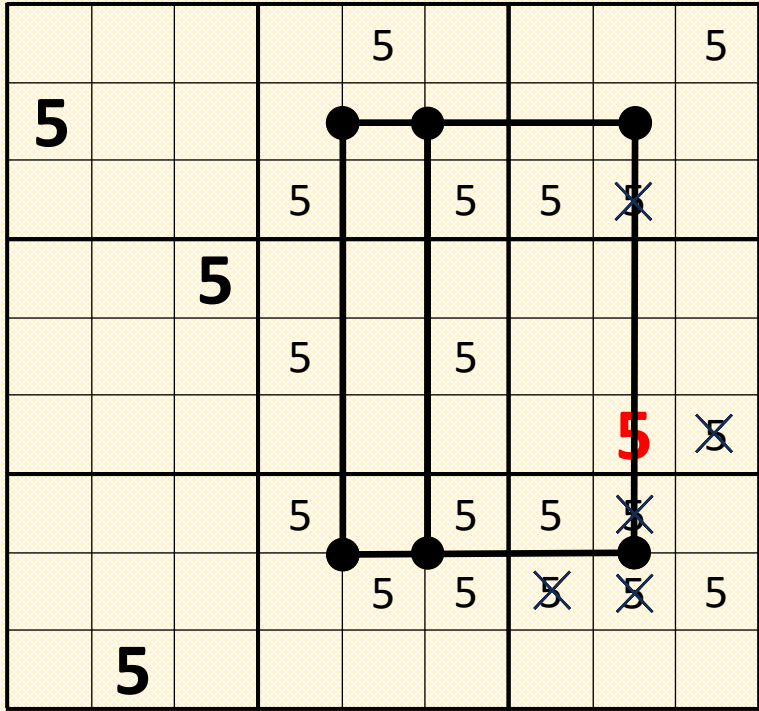


**Passback**

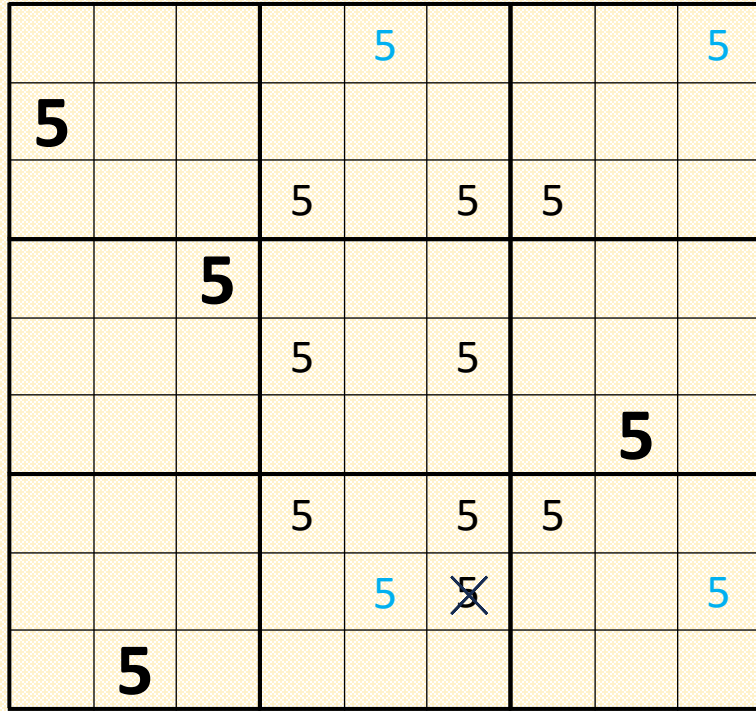
M63



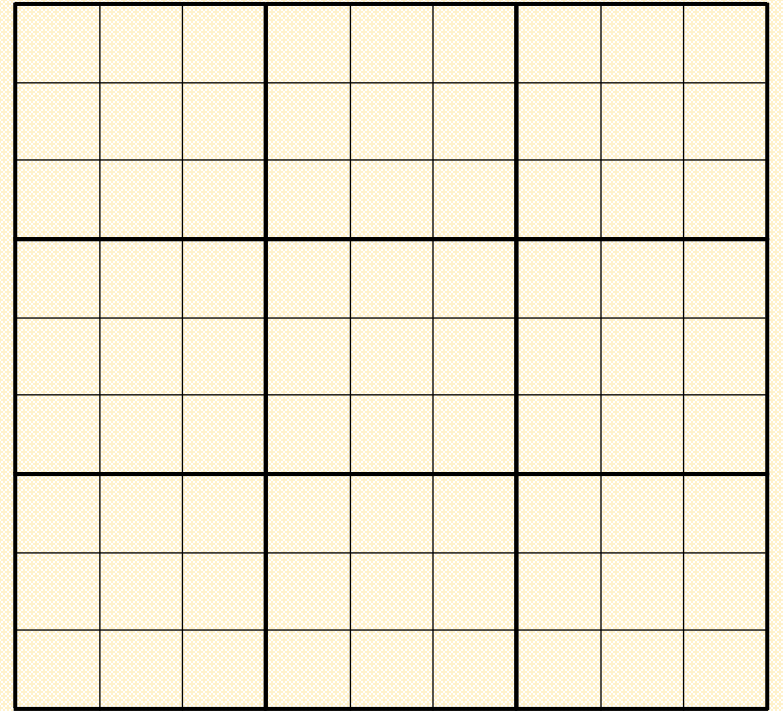
**MULTIPLE SERPENTS 2**



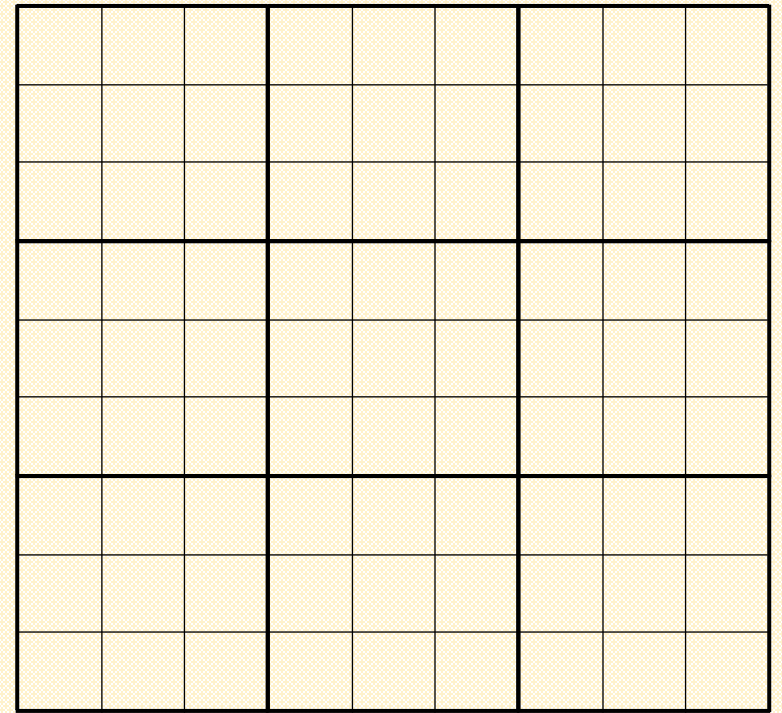
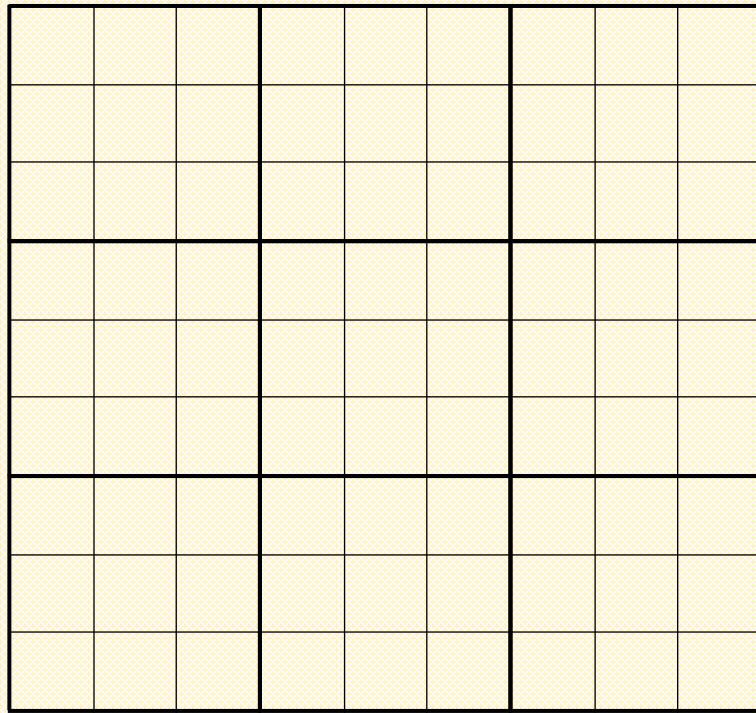
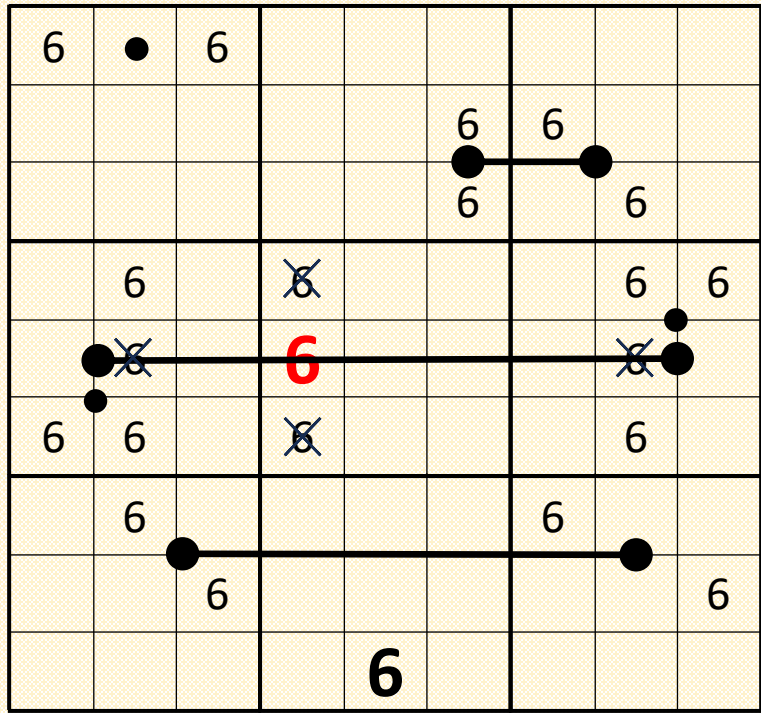
Step 1 - Possible Serpents



Step 2 - X-Wing



**MULTIPLE SERPENTS 3**



M72

The nodes are staggered in the columns of major squares but not in the rows. So, horizontal passthroughs are possible.

## STAGGERED NODES